



LEO

A Higher Order Theorem Prover



This work was supported by the Deutsche Forschungsgemeinschaft in Grant HOTEL and by the Studienstiftung des Deutschen Volkes

Extensional Higher Order Resolution

The Calculus

Higher Order Resolution

$$\frac{\text{KONSTRUKTIV} \quad \text{STRUKTIV} \quad \text{RESOLUTIV}}{\text{RESOLUTIV}} \quad \text{RESOLUTIV}$$

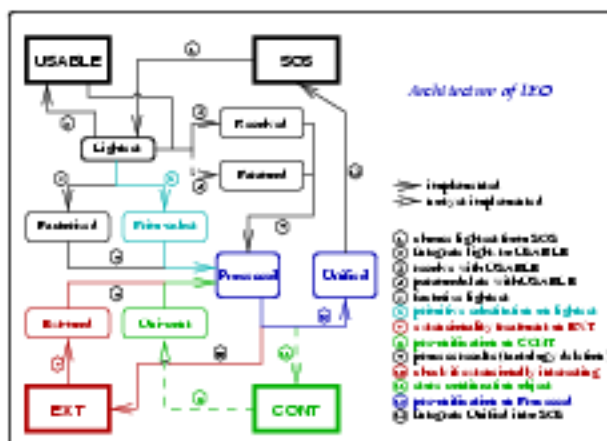
Higher Order Pre-Unification

$$\frac{\text{KONSTRUKTIV} \quad \text{STRUKTIV} \quad \text{RESOLUTIV}}{\text{RESOLUTIV}} \quad \text{RESOLUTIV}$$

Extensionality (Interleave Resolution and Unification)

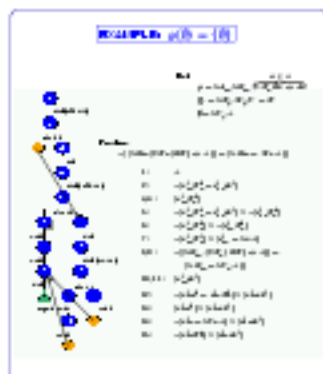
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Extended Set Of Support Architecture



Proving simple theorems about sets with LEO

Boolean and Basic Properties of Sets, Journal of Formalized Mathematics Volume 1, 1989



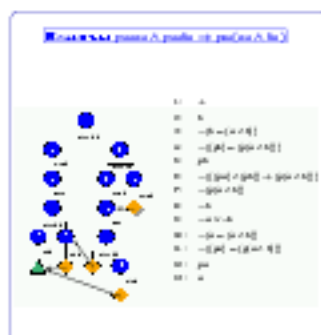
Technical Aspects of LEO

- Implemented in Allegro Common Lisp
- Based on the KEIM-Toolbox
- Automatic Mode
- Interactive Mode
- Graphical User Interface (LEO3)
- Integrated in OMEGA (LEO3)

Difficulties

- efficient Higher Order Subsumption
- Higher Order Term Indexing is not compatible with Extensional Resolution
- Leibnizequality or Primitive Equality

A very simple example with embedded Propositions



- not provable by other Systems

Conclusion and Further Work

- **LEO:** Henkin-Complete Extensional Higher Order Resolution
No Extensionality Axioms required
Interleaving of Resolution and Unification
Well suited for simple theorems from Set Theory
- **Further work:** More efficient implementation
Integration in OMEGA
Cooperation with other Reasoning Systems

Availability:

<http://www.ags.uni-sb.de/projects/deduktion/projects/hot/leo/>